

Massive Gauge Symmetries and Open/Closed Axion Mixing

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62(2014)115-151 with **Wieland Staessens**
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Motivation: Gauge Symmetries & Axions

- ▶ Type II string theory: a $U(1)$ per D-brane $\rightsquigarrow \sum_a U(1)_a$
 - ▶ few massless in 4D: $Y, B - L$
 - ▶ most massive in 4D: $U(1)_{PQ} \dots$
- ▶ $U(1)_{\text{massive}}$ remains as *perturbative* global symmetry



- ▶ non-pert: ~~$U(1)_{\text{massive}}$~~
 - ▶ $\mathbb{Z}_n \subset U(1)_{\text{massive}}$ survives
- \rightsquigarrow ultimate selection rules
on matter couplings in 4D

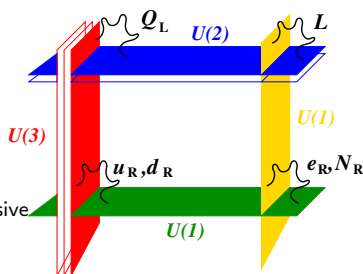
- ▶ explicit breaking by $\langle \phi_{\text{matter}} \rangle$
- \rightsquigarrow ~~$U(1)_{PQ}$~~ as solution to
strong CP problem

- ▶ Two kinds of **axions**:
 - ▶ Closed partner of (complex structure/Kähler) modulus & dilaton
 - ▶ Open: scalar matter with $U(1)_{\text{massive}}$ charge
- \rightsquigarrow mixing via Green-Schwarz coupling

Motivation: D-Brane Model Building

Spanish Quiver:

$$SU(3)_a \times SU(2)_b \times Y \times \begin{cases} U(1)_{\text{massive}}^3 \\ (B-L) \times U(1)_{\text{massive}}^2 \end{cases}$$



- ▶ 'Standard' realisation:

$$Y = \frac{Q_a}{6} + \frac{Q_c + Q_d}{2} \quad B - L = \frac{Q_a}{3} + Q_d$$

- ▶ $\mathbb{Z}_3 \subset U(1)_a$ automatic, but selection rules agree with $SU(3)_a$
 - ▶ non-trivial $\mathbb{Z}_n \subset \sum_{x \in \{a,b,c,d\}} k_x U(1)_x$ possible
 - ▶ generation dependent \mathbb{Z}_2 found in extension: $U(4) \times U(2)^4$
 - ▶ Natural candidate for $U(1)_{PQ}$ and axion σ :
 - ▶ $Q_L, L, (H_u, H_d), \sigma$ charged
 - ▶ $(u_R, d_R), (e_R, \nu_R)$ neutral
- $$\left. \begin{array}{l} \text{ } \\ \text{ } \end{array} \right\} U(1)_{PQ} = U(1)_b \text{ \& } \sigma = (\mathbf{Anti}_b)$$

- ▶ **Massive & discrete gauge symmetries**
 - ▶ Reminder of the Green Schwarz mechanism
 - ▶ \mathbb{Z}_n symmetries in global D-brane models
- ▶ **Axions, strong CP problem & the dark sector**
 - ▶ Open & closed string sector
 - ▶ ~~$U(1)_{PQ}$~~ & Higgs-axion potential in the DFSZ model
 - ▶ soft ~~SUSY~~ terms in D-brane models
 - ▶ Lower bounds on M_{string} in global D-brane models
- ▶ **Intermezzo: ~~SUSY~~ by deformations**
- ▶ **Conclusions**

Massive & Discrete Gauge Symmetries

- ▶ **Mixed anomalies** cancel by the **Green-Schwarz** mechanism:

$$\begin{array}{c}
 \text{U(1)}_a \\
 \text{SU(N}_b\text{)} \\
 \text{SU(N}_b\text{)}
 \end{array}
 +
 \begin{array}{c}
 \text{U(1)}_a \\
 \text{SU(N}_b\text{)} \\
 \text{SU(N}_b\text{)}
 \end{array}
 = 0$$

- ▶ **Axions** ξ_i ($\star_4 d\xi_i \sim dB_2^{(i)}$): longitudinal modes of $U(1)_{\text{massive}}^k$

$$\mathcal{S}_{CS} \supset \int_{\mathbb{R}^{1,3}} \sum_{i=0}^{h_{21}} \left(B_a^i \mathcal{B}_2^{(i)} \wedge \text{tr} F_a + A_b^i \xi_i \text{tr} F_b \wedge F_b \right)$$

with $\mathcal{B}_2^{(i)} \propto \int_{\Pi_i^{\text{odd}}} C_5^{RR}$; $\xi_i \propto \int_{\Pi_i^{\text{even}}} C_3^{RR}$

- ▶ $U(1)_X = \sum_a q_a U(1)_a$ **massless** if $\sum_a N_a q_a B_a^i = 0 \forall i$
- ▶ $\mathbb{Z}_n \subset U(1)_{\text{massive}}^k$ for suitable B_a^i ('mod n ') due to **shift symmetry** of ξ_i

Axionic Shift Symmetry - Type IIA Notation

- ▶ **Closed string axions** within $\mathcal{N} = 1$ chiral multiplets:

- ▶ axion-dilaton: $S = \phi + i\xi_0$

- ▶ complex structure: $U_i = c_i + i\xi_i$

- ▶ Kähler: $T_k = v_k + i b_k$

$$\xi_i \in C_3^{RR}$$

$$b_k \in B_2^{NSNS}$$

- ▶ $\mathcal{N} = 1$ **SUGRA action** independent of $\xi_i \rightarrow \xi_i + 1$

$$\mathcal{K}_{\text{closed}} = -\ln \Re(S) - \sum_i \ln \Re(U_i) - \sum_k \ln \Re(T_k)$$

- ▶ **perturbatively:** only couplings to $(\partial_\mu \xi_i)$

- ▶ **non-perturbative** couplings via D-brane instantons: $e^{-\mathcal{S}_{\text{inst}}}$

with $\mathcal{S}_{\text{inst}} \supset 2\pi i \xi_i$

in IIB: $U_i \leftrightarrow T_k$

- ▶ **Discrete \mathbb{Z}_n symmetry** preserved if

$$A^\mu \rightarrow A^\mu + \partial^\mu \lambda \quad \xi_i \rightarrow \xi_i + \underbrace{\bar{c}_i(B_a^i)}_{\text{mod } n} \lambda$$

$$0 \pmod n \quad \forall i$$

\rightsquigarrow need to determine $\bar{c}_i(B_a^i)!$

Green-Schwarz Couplings & \mathbb{Z}_n Symmetries - Type IIA

$$\mathcal{S}_{CS} \supset \int_{\mathbb{R}^{1,3}} \sum_{i=0}^{h_{21}} \left(B_a^i B_2^{(i)} \wedge \text{tr} F_a + A_b^i \xi_i \text{tr} F_b \wedge F_b \right)$$

with $B_2^{(i)} \propto \int_{\Pi_i^{\text{odd}}} C_5^{RR}$; $\xi_i \propto \int_{\Pi_i^{\text{even}}} C_3^{RR}$

- ▶ Expand 3-cycles and $\Omega\mathcal{R}$ -images as:

$$\Pi_a = \sum_{i=0}^{h_{21}} \left(A_a^i \Pi_i^{\text{even}} + B_a^i \Pi_i^{\text{odd}} \right), \quad \Pi'_a = \sum_{i=0}^{h_{21}} \left(A_a^i \Pi_i^{\text{even}} - B_a^i \Pi_i^{\text{odd}} \right)$$

- ▶ If $\Pi_i^{\text{even}} \circ \Pi_j^{\text{odd}} = m_i \delta_{ij}$ with $m_i \in \mathbb{Z} \rightsquigarrow dB_2^{(i)} = m_i \star_4 d\xi_i$
- ▶ $U(1) = \sum_a k_a U(1)_a \xrightarrow{\text{shift}} \xi_i \rightarrow \xi_i + \left(m_i \sum_a N_a k_a B_a^i \right) \lambda$
 - ▶ $\{\Pi_i^{\text{even}}, \Pi_j^{\text{odd}}\}$ span **sublattice** of finite index: $\Lambda_3^{\text{even}} \oplus \Lambda_3^{\text{odd}} \subsetneq \Lambda_3$
 - ▶ **all** known global D-brane models of **this type**
 - ▶ $A_a^i, B_a^i \in \frac{1}{m_i} \mathbb{Z}$
- ▶ resolve ambiguities (A_a^i, B_a^i) : rewrite '0 mod n ' as intersection $\#$

\mathbb{Z}_n Symmetries in Terms of Intersection Numbers - Type IIA

- ▶ ambiguities of normalisation factors m_i in B_a^i and Π_i^{odd} cancel

$U(1)_{\text{massless}} = \sum_a q_a U(1)_a$	$\mathbb{Z}_n \subset U(1)_{\text{massive}} = \sum_a k_a U(1)_a$
$\Pi_i^{\text{even}} \circ \sum_a N_a q_a \Pi_a = 0 \forall i$ $\Leftrightarrow \sum_a N_a q_a B_a^i = 0 \forall i$	$\Pi_i^{\text{even}} \circ \sum_a N_a k_a \Pi_a = 0 \pmod n \forall i$ $\Leftrightarrow m_i \sum_a N_a k_a B_a^i = 0 \pmod n \forall i$
$q_a \in \mathbb{Q}$	$k_a \in \mathbb{Z}, 0 \leq k_a < n, \text{gcd}(k_a, n) = 1$

- ▶ derivation of m_i, B_a^i for all **orbifolds** with particle physics models ✓
 - ▶ basis of $\{\Pi_i^{\text{even}}\}$ needed

$\rightsquigarrow \mathbb{Z}_n$ symmetries in any global model ✓

- ▶ **Cross-check:** K-theory constraint can be written as \mathbb{Z}_2 ✓

- ▶ **Bottom-up models:** $\{\Pi_i^{\text{even}}\}$ not known
 - ▶ use $(\Pi_x + \Pi'_x)_{x \in \{b,c,d\}} \circ \Pi_a = \Pi_x \circ (\Pi_a - \Pi'_a)$
 - ▶ **4 necessary conditions** (at most)
 - $\Leftrightarrow (h_{21} + 1)$ nec. + suff. conditions in global models
- ▶ **Redundant \mathbb{Z}_N symmetries:**
 - ▶ $\mathbb{Z}_N \subset U(1)_{\text{massive}} \subset U(N) \simeq SU(N)_{U(1)}$ automatic & trivial:

$$(\mathbf{N})_1 \quad (\mathbf{Adj})_0 + (\mathbf{1})_0 \quad (\mathbf{Sym})_2 + (\mathbf{Anti})_2$$

- ▶ **But:** non-trivial sums of $\mathbb{Z}_{N_a} \subset U(N_a)$ charges can arise
 \rightsquigarrow **generation dependent \mathbb{Z}_n symmetries**

example of generation dependent \mathbb{Z}_2 later

SUSY field theory:

- ▶ *Discrete gauge symmetries and the origin of baryon and lepton number conservation in supersymmetric versions of the standard model* L.E.Ibáñez, G.G.Ross: Nucl.Phys.B368(1992)3-37
- ▶ *What is the discrete gauge symmetry of the MSSM?*
H.K.Dreiner, C.Luhn, M.Thormeier: Phys.Rev.D73(2006)075007

↪ R-parity (\mathbb{Z}_2), baryon triality (\mathbb{Z}_3), proton hexality (\mathbb{Z}_6) for e.g.

proton stability

D-brane models:

- ▶ *Discrete gauge symmetries in D-brane models* M.Berasaluce-Gonzalez, L.E.Ibáñez, P.Soler, A.M.Uranga: JHEP1112(2011)113
- ▶ *Discrete Gauge Symmetries in Discrete MSSM-like Orientifolds*
L.E.Ibáñez, A.N.Schellekens, A.M.Uranga: Nucl.Phys.B865(2012)509-540
- ▶ *String Constraints on Discrete Symmetries in MSSM Type II Quivers* P.Anastasopoulos, M.Cvetič, R.Richter, P.K.S.Vaudrevange: JHEP1303(2013)011
- ▶ *Z_p charged branes in flux compactifications* M.Berasaluce-Gonzalez, P.G.Camara, F.Marchesano, A.M.Uranga: JHEP1304(2013)138

▶

...

GH, W. Staessens '13

- ▶ $\dim(\Lambda_3^{\text{even}}) = h_{21} + 1$ conditions
- ▶ phenomenologically interesting:

- ▶ T^6/\mathbb{Z}_6 : $h_{21} = 5$
- ▶ T^6/\mathbb{Z}'_6 : $h_{21} = 5 (+6)^*$
- ▶ $T^6/\mathbb{Z}_2 \times \mathbb{Z}_6$: $h_{21} = 15 (+4)^*$
- ▶ $T^6/\mathbb{Z}_2 \times \mathbb{Z}_6$: $h_{21} = 15$

* D-branes wrap only untwisted & \mathbb{Z}_2 twisted cycles

- ▶ shape of Λ_3^{even} depends on lattice orientations under $\Omega\mathcal{R}$
- ▶ L-R symmetric & Pati-Salam models '*natural*' on D-branes
 $\rightsquigarrow U(1)_Y$ (SM) & $U(1)_{B-L}$ (L-R) to rotate charges to 0

Example I: L-R Symmetric Model on T^6/\mathbb{Z}_6

GH, Ott '04; see also Gmeiner, GH '09

- ▶ $U(3)_a \times U(2)_b \times USp(2)_c \times U(1)_d \times USp(2)_e$
- ▶ $U(1)_{B-L} = (\frac{Q_a}{3} + Q_d)_{\text{massless}} \ \& \ U(1)_{\text{massive}}^2$
- ▶ $USp(2)_{x \in \{c, e\}} \rightarrow U(1)_{x, \text{massless}}$ by brane displacement
- ▶ only $x \in \{a, b, d\}$ contribute to \mathbb{Z}_n conditions
- ▶ after $B - L$ rotation:

GH, Staessens '13

Discrete sym.		Charge assignment for the MSSM states									
\mathbb{Z}_n	$\subset \sum_x k_x U(1)_x$	Q_L	\bar{U}_R	\bar{D}_R	L	\bar{E}_R	\bar{N}_R	$H_u^{(1)}$	$H_u^{(2)}$	$H_d^{(1)}$	$H_d^{(2)}$
\mathbb{Z}_2	$Q_a + Q_d$	0	0	0	0	0	0	0	0	0	0
\mathbb{Z}_2	Q_b	0	1	1	0	1	1	1	1	1	1
\mathbb{Z}_3	Q_a	0	0	0	0	0	0	0	0	0	0

not listed: mild amount of vector-like exotics

- ▶ $(k_a, k_b, k_d) = (1, 1, 1) \simeq \mathbb{Z}_2$ of K-theory constraint
- ▶ $\mathbb{Z}_2^{(b)}$ gives **no extra constraints** beyond $SU(2)_b$ charges
 \rightsquigarrow **all \mathbb{Z}_n appear trivial from 4D perspective**

Example II: L-R Symmetric Model on T^6/\mathbb{Z}'_6

Gmeiner, GH '07-'08

- ▶ $U(3)_a \times U(2)_b \times USp(2)_c \times U(1)_d$ ($\times USp(6)_{\text{hidden}}$)
- ▶ $U(1)_{B-L} = (\frac{Q_a}{3} + Q_d)_{\text{massless}} \ \& \ U(1)_{\text{massive}}^2$
- ▶ $USp(2)_c \rightarrow U(1)_{c,\text{massless}}$ by brane displacement σ
- ▶ $USp(6)_{\text{hidden}}$ **cannot** be broken by σ or τ (SUSY)
- ▶ after $B-L$ rotation:

GH, Staessens '13

Discrete sym.		Charge assignment for the chiral states									
\mathbb{Z}_n	$\subset \sum_x k_x U(1)_x$	Q_L	\bar{U}_R	\bar{D}_R	L	\bar{L}	\bar{E}_R	\bar{N}_R	H_u	H_d	Σ_b
\mathbb{Z}_2	$Q_a + Q_d$	0	0	0	0	0	0	0	0	0	0
\mathbb{Z}_3	Q_a	0	0	0	0	0	0	0	0	0	0
\mathbb{Z}_6	Q_b	0	1	1	4	4	3	3	5	5	4
	$\xrightarrow{U(1)_c}$	0	0	2	4	4	4	2	0	4	4

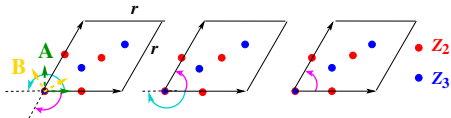
open string axion: $\Sigma_b \simeq (\mathbb{1}_{\text{Anti}_b})_{-2_b}$

not listed: mild amount of vector-like exotics

- ▶ **non-trivial:** $\mathbb{Z}_3 \subset U(1)_b$

Example III: A Pati-Salam Model on $T^6/\mathbb{Z}_2 \times \mathbb{Z}'_6$

- $\mathbb{Z}_2 \times \mathbb{Z}'_6$ shifts: $\vec{v} = (\frac{1}{2}, \frac{-1}{2}, 0)$, $\vec{w}' = (\frac{-1}{3}, \frac{1}{6}, \frac{1}{6})$ on $SU(3)^3$



- $\Pi_a^{\text{frac}} = \frac{1}{4} (X_a \rho_1 + Y_a \rho_2 + \sum_{k=1}^3 \sum_{\alpha=1}^5 [X_{a,\alpha}^{(k)} \varepsilon_{\alpha}^{(k)} + y_{a,\alpha}^{(k)} \tilde{\varepsilon}_{\alpha}^{(k)}])$
with $\rho_1 \circ \rho_2 = -\varepsilon_{\alpha}^{(k)} \circ \tilde{\varepsilon}_{\alpha}^{(k)} = 4$

- $\Omega\mathcal{R}$ -even & odd 3-cycles:

GH, Staessens '13

$$\Pi_0^{\text{even}, \mathbf{I}} = \rho_1,$$

$$\Pi_{\alpha \in \{1,2,3\}}^{\text{even}, \mathbb{Z}_2^{(k)}} = \varepsilon_{\alpha}^{(k)},$$

$$\Pi_4^{\text{even}, \mathbb{Z}_2^{(k)}} = \varepsilon_4^{(k)} + \varepsilon_5^{(k)},$$

$$\Pi_5^{\text{even}, \mathbb{Z}_2^{(k)}} = 2(\tilde{\varepsilon}_4^{(k)} - \tilde{\varepsilon}_5^{(k)}) - (\varepsilon_4^{(k)} - \varepsilon_5^{(k)}),$$

$$\Pi_0^{\text{odd}, \mathbf{I}} = -\rho_1 + 2\rho_2,$$

$$\Pi_{\alpha \in \{1,2,3\}}^{\text{odd}, \mathbb{Z}_2^{(k)}} = -\varepsilon_{\alpha}^{(k)} + 2\tilde{\varepsilon}_{\alpha}^{(k)},$$

$$\Pi_4^{\text{odd}, \mathbb{Z}_2^{(k)}} = 2(\tilde{\varepsilon}_4^{(k)} + \tilde{\varepsilon}_5^{(k)}) - (\varepsilon_4^{(k)} + \varepsilon_5^{(k)}),$$

$$\Pi_5^{\text{odd}, \mathbb{Z}_2^{(k)}} = \varepsilon_4^{(k)} - \varepsilon_5^{(k)},$$

- Intersection numbers

$$\Pi_{\tilde{\alpha}}^{\text{even}, \mathbb{Z}_2^{(k)}} \circ \Pi_{\tilde{\beta}}^{\text{odd}, \mathbb{Z}_2^{(l)}} = \delta^{kl} \delta_{\tilde{\alpha}\tilde{\beta}} \times \begin{cases} 8 & \tilde{\alpha} = 0 \\ -8 & 1 \dots 3 \\ -16 & 4 \\ 16 & 5 \end{cases} \quad \text{with } \mathbb{Z}_2^{(0)} \equiv \mathbf{1}$$

- wrapping numbers a priori $A_a^i, B_a^i \in \frac{1}{8} \mathbb{Z}$

A Pati-Salam Model on $T^6/\mathbb{Z}_2 \times \mathbb{Z}'_6: \mathbb{Z}_n$ Conditions

$$\sum_a k_a N_a \left(\begin{array}{c} Y_a \\ -y_{a,1}^{(1)} \\ -y_{a,2}^{(1)} \\ -y_{a,3}^{(1)} \\ -(y_{a,4}^{(1)} + y_{a,5}^{(1)}) \\ 2(x_{a,4}^{(1)} - x_{a,5}^{(1)}) + (y_{a,4}^{(1)} - y_{a,5}^{(1)}) \\ \hline -y_{a,1}^{(2)} \\ -y_{a,2}^{(2)} \\ -y_{a,3}^{(2)} \\ -(y_{a,4}^{(2)} + y_{a,5}^{(2)}) \\ 2(x_{a,4}^{(2)} - x_{a,5}^{(2)}) + (y_{a,4}^{(2)} - y_{a,5}^{(2)}) \\ \hline -y_{a,1}^{(3)} \\ -y_{a,2}^{(3)} \\ -y_{a,3}^{(3)} \\ -(y_{a,4}^{(3)} + y_{a,5}^{(3)}) \\ 2(x_{a,4}^{(3)} - x_{a,5}^{(3)}) + (y_{a,4}^{(3)} - y_{a,5}^{(3)}) \end{array} \right) \stackrel{!}{=} 0 \pmod n \stackrel{!}{=} \sum_a k_a N_a$$

$$\left(\begin{array}{c} \frac{Y_a - \sum_{i=1}^3 [y_{a,1}^{(i)} + y_{a,2}^{(i)} + y_{a,3}^{(i)}]}{4} \\ \frac{Y_a - [y_{a,1}^{(1)} + y_{a,2}^{(1)} + y_{a,3}^{(1)}]}{2} \\ \frac{Y_a - [y_{a,1}^{(2)} + y_{a,2}^{(2)} + y_{a,3}^{(2)}]}{2} \\ \frac{y_{a,1}^{(2)} + y_{a,3}^{(2)} + y_{a,1}^{(3)} + y_{a,3}^{(3)}}{2} \\ \frac{y_{a,1}^{(1)} + y_{a,3}^{(1)} + y_{a,2}^{(2)} + y_{a,3}^{(2)}}{2} \\ \frac{y_{a,2}^{(1)} + y_{a,3}^{(1)} + y_{a,2}^{(2)} + y_{a,3}^{(2)}}{2} \\ \hline \frac{Y_a + [y_{a,3}^{(1)} + x_{a,4}^{(1)} + y_{a,4}^{(1)} - x_{a,5}^{(1)}] + \sum_{j=2}^3 [y_{a,2}^{(j)} - (y_{a,4}^{(j)} + y_{a,5}^{(j)})]}{4} \\ \frac{Y_a + \sum_{j=1,2} [y_{a,1}^{(j)} - x_{a,4}^{(j)} + x_{a,5}^{(j)} + y_{a,5}^{(j)}] + [y_{a,3}^{(3)} + x_{a,4}^{(3)} + y_{a,4}^{(3)} - x_{a,5}^{(3)}]}{4} \\ \frac{Y_a + [y_{a,2}^{(2)} - (y_{a,4}^{(2)} + y_{a,5}^{(2)})]}{2} \\ \frac{Y_a + [y_{a,1}^{(1)} - x_{a,4}^{(1)} + x_{a,5}^{(1)} + y_{a,5}^{(1)}]}{2} \\ \frac{y_{a,4}^{(2)} + y_{a,5}^{(2)} + y_{a,4}^{(3)} + y_{a,5}^{(3)}}{2} \\ \frac{-x_{a,4}^{(1)} - x_{a,5}^{(1)} + y_{a,5}^{(1)} + x_{a,4}^{(2)} - x_{a,5}^{(2)} + y_{a,5}^{(2)}}{2} \\ \hline \frac{Y_a + \sum_{i=1}^3 [y_{a,3}^{(i)} + x_{a,4}^{(i)} + y_{a,4}^{(i)} - x_{a,5}^{(i)}]}{4} \\ \frac{Y_a + y_{a,3}^{(1)} + x_{a,4}^{(1)} + y_{a,4}^{(1)} - x_{a,5}^{(1)}}{4} \\ \frac{Y_a + y_{a,3}^{(2)} + x_{a,4}^{(2)} + y_{a,4}^{(2)} - x_{a,5}^{(2)}}{2} \\ \frac{Y_a + \sum_{i=1}^3 y_{a,3}^{(i)}}{2} \end{array} \right)$$

A Pati-Salam Model on $T^6/\mathbb{Z}_2 \times \mathbb{Z}'_6$: Spectrum

GH, Ripka, Staessens '12

$$SU(4)_a \times SU(2)_b \times SU(2)_c \times SU(2)_d \times SU(2)_e \times U(1)_{\text{massive}}^5$$

- ▶ Standard Model particles plus **one Higgs**

$$(4, \bar{2}, 1; 1, 1) + 2(4, 2, 1; 1, 1) + (\bar{4}, 1, 2; 1, 1) + 2(\bar{4}, 1, \bar{2}; 1, 1) + (1, 2, \bar{2}; 1, 1)$$

\rightsquigarrow **one massive generation** at leading order
by charge selection rules

- ▶ chiral w.r.t. anomalous $U(1)_{\text{massive}}^5$

$$(1, 2, 1; \bar{2}, 1) + 3(1, \bar{2}, 1; \bar{2}, 1) + (1, \bar{2}, 1; 1, \bar{2}) + (1, 1, \bar{2}; 2, 1) + 3(1, 1, 2; 2, 1) + (1, 1, 2; 1, 2)$$

but non-chiral w.r.t. $SU(4)_a \times SU(2)_b \times SU(2)_c$

- ▶ non-chiral w.r.t. to full $U(4)_a \times U(2)^4$ with **GUT Higgses**

$$2[(4, 1, 1; \bar{2}, 1) + h.c.] + [(1, 1, 1; 2, 2) + h.c.] + (1, 1, 1; 4_{\text{Adj}}, 1) \\ + 2[(1, 1, 1; 3_S, 1) + (1, 1, 1; 1_A, 1) + h.c.] + [(1, 1, 1; 1, 3_S) + (1, 1, 1; 1, 1_A) + h.c.]$$

Pati-Salam model cont'd: \mathbb{Z}_n Symmetries in $U(1)_{\text{massive}}^5$

- ▶ 5 independent \mathbb{Z}_n symmetries ($h_{21} = 15$)
- ▶ 4 family-independent & trivial: $\mathbb{Z}_N \subset U(N)$

G.H., Staessens '13

▶ **family-dependent:**

- ▶ $\mathbb{Z}_4 \subset \frac{1}{2} \sum_{x \in \{b,c,d,e\}} U(1)_x \rightsquigarrow$ **selection rule on Yukawas**

Discrete charges for the five-stack Pati-Salam model on $T^6/(\mathbb{Z}_2 \times \mathbb{Z}'_6 \times \Omega\mathcal{R})$

Discrete symmetries		Charge assignment for the 'chiral' states										
\mathbb{Z}_n	$U(1) = \sum_x k_x U(1)_x$	(Q_L, L) $ab \quad ab'$		(Q_R, R) $ac \quad ac'$		(H_d, H_u)	X_{bd}	$X_{bd'}$	$X_{be'}$	X_{cd}	$X_{cd'}$	$X_{ce'}$
\mathbb{Z}_2	$U(1)_e$	0	0	0	0	0	0	0	1	0	0	1
	$U(1)_d$	0	0	0	0	0	1	1	0	1	1	0
	$U(1)_c$	0	0	1	1	1	0	0	0	1	1	1
	$U(1)_b$	1	1	0	0	1	1	1	1	0	0	0
\mathbb{Z}_4	$U(1)_a$	1	1	3	3	0	0	0	0	0	0	0
	$U(1)_b + U(1)_c + U(1)_d + U(1)_e$	3	1	1	3	0	0	2	2	0	2	2

Reduction of the *Family Dependent Symmetry*: $\mathbb{Z}_4 \rightarrow \mathbb{Z}_2$

- ▶ unwritten lore: **mod out centers** of $SU(N)$:
 $((\mathbb{Z}_4)^2 \times (\mathbb{Z}_2)^3)/(\mathbb{Z}_4 \times (\mathbb{Z}_2)^4) \simeq \mathbb{Z}_2$
- ▶ search consistent charge assignment by hand:
 - ▶ $(4, \bar{2}, 1, 1, 1) \cdot (\bar{4}, 1, 2, 1, 1) \cdot (1, 2, \bar{2}, 1, 1)$ *perturbatively* allowed
 - ▶ $(4, \bar{2}, 1, 1, 1) \cdot (\bar{4}, 1, 1, 2, 1) \cdot (1, \bar{2}, 1, \bar{2}, 1)$ *pert.* forbidden by $U(1)_b$
 - \mathbb{Z}_4 charge: $2 \bmod 4$
 - ▶ $(4, \bar{2}, 1, 1, 1) \cdot (\bar{4}, 1, \bar{2}, 1, 1) \cdot (1, 2, \bar{2}, 1, 1)$ *pert.* forbidden by $U(1)_c$
 - ▶ ...

	(Q_L, L)		(Q_R, R)		(H_d, H_u)	X_{bd}	$X_{bd'}$	$X_{be'}$	X_{cd}	$X_{cd'}$	$X_{ce'}$
	ab	ab'	ac	ac'							
\mathbb{Z}_2	0	1	0	1	0	0	1	1	0	1	1

- ▶ \mathbb{Z}_2 remains **family-dependent**
 ... *very special D-brane configuration*
- ▶ **cannot** be obtained from 'mod 2' on \mathbb{Z}_4 charges
 \rightsquigarrow unwritten lore doesn't really help

Axions, Strong CP Problem, Dark Sector

Axions and the Strong CP Problem

- ▶ **Axions** originally invoked to solve **strong CP-problem**

$$\mathcal{L}_\alpha \supset \frac{1}{2} (\partial_\mu \alpha) (\partial^\mu \alpha) - \frac{1}{32\pi^2} \frac{\alpha(x)}{f_\alpha} \text{Tr}(G_{\mu\nu} \tilde{G}^{\mu\nu})$$

- ▶ *global* Pecci-Quinn symmetry $U(1)_{PQ}$ Pecci, Quinn '77
- ▶ **axion** α arises from rewriting two Higgs doublets
- ▶ ~~electro-weak~~ & ~~PQ~~ scales identical
- ▶ axions \leftrightarrow photon conversion assumed (*Primakoff effect*)
 \rightsquigarrow astrophysical & lab searches (e.g. ALPs@DESY)
experimentally excluded
- ▶ modified models contain **SM singlet field** σ
 - ▶ σ couples to Higgs doublets \rightsquigarrow new terms in V_{Higgs}
 - ▶ ~~PQ~~ by $\langle \sigma \rangle$ at higher energy than ~~$SU(2)_L \times U(1)_Y$~~

e.g. Zhitnitsky '80; Dine, Fischler, Srednicki '81; ...; Dreiner, Staub, Ubaldi '14

► realisation in **D-brane models**

- open string axions cf. Berenstein, Perkins '12
- $U(1)_{PQ} \rightarrow U(1)_{\text{massive}}$
- 'exotic' scalars abundant - adjustments to **SUSY** required
- suitable SUSY breaking minimum of V_{Higgs} ?

GH, Staessens '13

Open String Axions & DFSZ Model

- ▶ $U(1)_{PQ}$ must allow:

$$\mathcal{L}_{\text{Yukawa}} = f_u Q_L \cdot H_u u_R + f_d Q_L \cdot H_d d_R + f_e L \cdot H_d e_R + f_\nu L \cdot H_u \nu_R$$

- ▶ introduce **SM singlet** σ with $U(1)_{PQ} \simeq U(1)_{\text{massive}}$ charge
- ▶ (H_u, H_d) charged under $U(1)_{PQ}$
 $\rightsquigarrow Q_L$ or (u_R, d_R) have $U(1)_{PQ}$ charge

- ▶ **Higgs potential** of the DFSZ model

$$\begin{aligned} V_{\text{DFSZ}}(H_u, H_d, \sigma) = & \lambda_u (H_u^\dagger H_u - v_u^2)^2 + \lambda_d (H_d^\dagger H_d - v_d^2)^2 + \lambda_\sigma (\sigma^* \sigma - v_\sigma^2)^2 \\ & + (a H_u^\dagger H_u + b H_d^\dagger H_d) \sigma^* \sigma + c (H_u \cdot H_d \sigma^2 + \text{h.c.}) \\ & + d |H_u \cdot H_d|^2 + e |H_u^\dagger H_d|^2 \end{aligned}$$

- ▶ **SUSY** version: $V = V_F + V_D + V_{\text{soft}}$
- ▶ modify $c (H_u \cdot H_d \sigma^2 + \text{h.c.}) \longrightarrow c (H_u \cdot H_d \sigma + \text{h.c.})$; $\sigma \sim e^{ia}$

Matter	Q_L	\bar{u}_R	\bar{d}_R	H_u	H_d	L	\bar{e}_R	$\bar{\nu}_R$	Σ
$U(1)_{PQ}$	∓ 1	0	0	± 1	± 1	∓ 1	0	0	∓ 2

- ▶ identify $\Sigma = (\text{Anti})_{U(2)_b}$ in global D-brane model

e.g. SM on T^6/\mathbb{Z}_6 : GH, Ott '04 & T^6/\mathbb{Z}'_6 : Gmeiner, GH '08

Mixing of Open and Closed String Axions

GH, Staessens '13

- ▶ open string axion a from $\sigma = \frac{v+s(x)}{\sqrt{2}} e^{i\frac{a(x)}{v}}$
- ▶ **open** axion a mixes with **closed** axion ξ ($\leftarrow U(1)_{\text{massive}}$)

$$\zeta = \frac{M_{\text{string}} \xi + qv a}{\sqrt{M_{\text{string}}^2 + q^2 v^2}}, \quad \alpha = \frac{M_{\text{string}} a - qv \xi}{\sqrt{M_{\text{string}}^2 + q^2 v^2}}$$

$$\Rightarrow \mathcal{L}_{\text{CP-odd}} = \frac{1}{2} (\partial_\mu \zeta + m_B B_\mu)^2 + \frac{1}{2} (\partial_\mu \alpha)^2$$

- ▶ axion **decay constant** f_α from dim. reduction:

$$\mathcal{L}_{\text{anom}} = \frac{1}{16\pi^2} \frac{\zeta(x)}{f_\zeta} \text{Tr}(G_{\mu\nu} \tilde{G}^{\mu\nu}) + \frac{1}{32\pi^2} \frac{\alpha(x)}{f_\alpha} \text{Tr}(G_{\mu\nu} \tilde{G}^{\mu\nu})$$

$$\text{with } f_\zeta = \frac{\sqrt{M_{\text{string}}^2 + (qv)^2}}{2}, \quad f_\alpha = \frac{M_{\text{string}} qv \sqrt{M_{\text{string}}^2 + (qv)^2}}{(M_{\text{string}}^2 - (qv)^2)}$$

- ▶ For $M_{\text{string}} \gg v$: $\zeta \simeq \xi_{\text{closed}}, \alpha \simeq a_{\text{open}}$

Soft SUSY Terms

Origin of $V = V_F + V_D + V_{\text{soft}}$

$$\begin{aligned} V_{\text{DFSZ}}(H_u, H_d, \sigma) &= \lambda_u (H_u^\dagger H_u - v_u^2)^2 + \lambda_d (H_d^\dagger H_d - v_d^2)^2 + \lambda_\sigma (\sigma^* \sigma - v_\sigma^2)^2 \\ &+ (a H_u^\dagger H_u + b H_d^\dagger H_d) \sigma^* \sigma + c (H_u \cdot H_d \sigma + h.c.) \\ &+ d |H_u \cdot H_d|^2 + e |H_u^\dagger H_d|^2 \end{aligned}$$

in **SUSY field theory**

- ▶ $\mathcal{W} = \mu \Sigma H_d \cdot H_u$
- ▶ $K^{\text{SUSY}}(\Phi^\dagger e^{2gV} \Phi) = \Phi^\dagger e^{2gV} \Phi$
- ▶ $\mathcal{W}_{\text{soft}} = \eta c H_u \cdot H_d \Sigma \rightsquigarrow \mathcal{A}\text{-terms}$
- ▶ $K_{\text{soft}} = \eta \bar{\eta} m_\Phi^2 \Phi^\dagger e^{2gV} \Phi \rightsquigarrow m_{\text{soft}}$

in **Type II string models**

- ▶ strongly coupled hidden group e.g. $USp(6)$ in T^6/\mathbb{Z}'_6 model
- ▶ gaugino condensate: $\langle \lambda \lambda \rangle = \Lambda_c^3 \rightsquigarrow M_{\text{SUSY}}^2 = \langle F^{\mathcal{H}} \rangle \sim \frac{\Lambda_c^3}{M_{\text{Planck}}}$
- ▶ gravity (+ gauge) mediation to SM sector

Lower Bounds on M_{string}

- ▶ typical phenomenological constraints from $f_\zeta \sim M_{\text{string}}$, $f_\alpha \sim qv$: $M_{\text{string}} \geq 10^9$ GeV
 - ▶ supplemented by constraints on gauge couplings
 - ▶ $\frac{M_{\text{Planck}}^2}{M_{\text{string}}^2} = \text{examples } \frac{4\pi v_1 v_2 v_3}{g_{\text{string}}^2}$
 - ▶ @ tree-level: $\frac{4\pi}{g_{SU(N_a)}^2} = \frac{\sqrt{v_1 v_2 v_3}}{8\pi^3 3^{1/4} g_{\text{string}}} \times \mathcal{O}(1)_{\text{model}}$
 - ▶ @ 1-loop: linear dep. on v_i , $\ln \frac{v_1 v_3}{v_2^2} \leftarrow$ cancellations possible
- $\rightsquigarrow M_{\text{string}}$ can be lowered to intermediary scale by exponentially large volumes:

GH, Staessens '13

M_{string} as a function of v_i and g_{string}								
$g_{\text{string}} = 0.1$			$g_{\text{string}} = 0.01$			$g_{\text{string}} = 0.001$		
$v_1 v_3$	$v_{2,\text{max}}^2$	M_{string}	$v_1 v_3$	$v_{2,\text{max}}^2$	M_{string}	$v_1 v_3$	$v_{2,\text{max}}^2$	M_{string}
10^8	9.7×10^9	1.6×10^{10} GeV	10^6	1.5×10^{10}	1.6×10^{10} GeV	10^2	1.5×10^6	1.6×10^{12} GeV
10^{10}	1.5×10^{14}	2.8×10^9 GeV	10^8	1.6×10^{14}	1.5×10^8 GeV	10^4	1.6×10^{10}	1.5×10^{10} GeV
10^{12}	1.5×10^{18}	2.8×10^8 GeV	10^{10}	1.6×10^{18}	1.5×10^6 GeV	10^6	1.6×10^{14}	1.5×10^8 GeV

~~SUSY~~ by Deformations

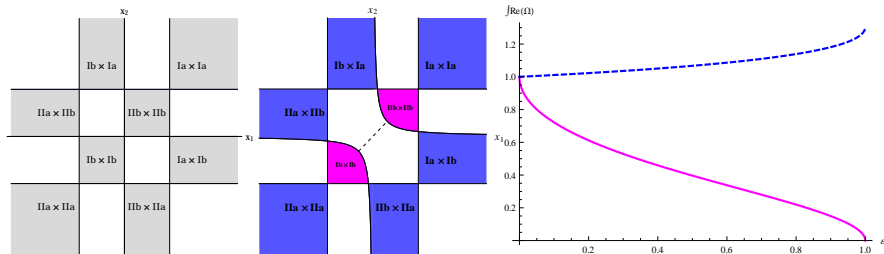
- ▶ What happens to $\text{Vol}_{\text{brane}}(\Pi)$ if \mathbb{Z}_2 singularities are deformed?
- ▶ use product of \mathbb{P}_{112}^2 with coord. (x_i, v_i, y_i) and for square tori $F_i = x_i v_i (x_i^2 - v_i^2)$

$$(T^2)^3 / \mathbb{Z}_2 \times \mathbb{Z}_2 \simeq \{f = -y^2 + F_1 F_2 F_3 = 0\} \quad \text{with } y \equiv y_1 y_2 y_3$$

- ▶ a **single** deformed fixed point:
 $f = -y^2 + F_1 F_2 F_3 + \varepsilon \delta F_1 \delta F_2 \cdot F_3 = 0 \rightsquigarrow y = y(x_1, x_2, x_3, \varepsilon)|_{v_i=1}$
- ▶ use $\Omega_3 = dz_1 dz_2 dz_3$ on $(T^2)^3$ with relation $dz_i = \frac{dx_i}{y_i}$
- ▶ compute $\int_{\Pi} \Omega_3 = \int_{\Pi} \frac{dx_1 dx_2 dx_3}{y}$ for deformed geometry:
 - ▶ decrease with $\sqrt{\varepsilon}$ if Π contains singularity
 - ▶ change linear in ε otherwise

Visualisation of Deformation of Singularity along $T_1^2 \times T_2^2$

- ▶ deformation of singularity at $x_1 = x_2 = 0$ along $T_1^2 \times T_2^2$



- ▶ volume of 3-cycle passing through singularity changes $\sim -\sqrt{\varepsilon}$

$$y = \sqrt{(x_1^2 - 1)(x_2^2 - 1)(x_1 x_2 + \varepsilon)x_3(x_3^2 - 1)}$$

$$\int_{\Pi} \Omega_3 = \int_{\Pi} \frac{dx_1 dx_2 dx_3}{y} \stackrel{\text{SUSY}}{=} \int_{\Pi} \Re(\Omega_3)$$

- ▶ $\varepsilon > 0$ $\Pi_a^{\mathbb{Z}_2} = \Pi_{a'}$, $SO(2N)$ & $USp(2N)$ branes stay SUSY
- ▶ $\varepsilon < 0$ $\Pi_a^{\mathbb{Z}_2} = -\Pi_{a'}$, SUSY on $U(N)$ branes

i.e. orbifold point is only SUSY point of SM branes

Conclusions:

- ▶ \mathbb{Z}_n expressed via **intersection numbers** in Type IIA:
 - ▶ $(h_{21} + 1)$ nec. + suf. conditions per orbifold
 - ▶ many \mathbb{Z}_n trivial in 4D field theory (e.g. $\mathbb{Z}_N \subset U(N)$)
 - ▶ **family-dependent** \mathbb{Z}_4 (\mathbb{Z}_2) constrains Yukawas

... details in **GH**, Staessens '13

- ▶ $U(1)_{PQ} \simeq U(1)_{\text{massive}}$ and axions as (**Anti**) $_{U(2)}$
 - ▶ Mixing of **axions** from open/closed string sector
 - ▶ ~~$U(1)_{PQ}$~~ and ~~$SU(2) \times Y$~~ scales decouple
 - ▶ intermediary M_{string} and exponentially large volumes

... to be explored in greater detail

... details in **GH**, Staessens '13

- ▶ ~~SUSY~~ by deformation of 3-cycles
- ... how are SM fields affected?

... details in Blaszczyk, **GH**, Koltermann '14

Registration ends 31 July

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Massive Gauge Symmetries and Open/Closed Axion Mixing